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# MOLECULAR MODELING OF HIGH-TEMPERATURE OXIDATION OF REFRACTORY BORIDES

FA9550-05-1-0026

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## Abstract

Refractory diboride with silicon carbide additive has a unique oxide scale structure with two condensed oxide phases (solid + liquid), and demonstrates oxidation resistance superior to either monolithic diboride or silicon carbide. We rationalize that this is because the silica-rich liquid phase can retreat outward to remove the high SiO gas volatility region, while still holding onto the zirconia skeleton mechanically by capillary forces, to form a "solid pillars, liquid roof" scale architecture and maintain barrier function. Basic assessment of the oxygen carriers in the borosilicate liquid in oxygen-rich condition is performed based on first-principles calculations. It is estimated from entropy and mobility arguments that above a critical temperature  $T_C \sim 1500^\circ\text{C}$ , the dominant oxygen carriers should be network defects, such as peroxy linkage or oxygen deficient centers, instead of molecular  $\text{O}_2^*$  as in the Deal-Grove model. These network defects will lead to sub-linear dependence of the oxidation rate with external oxygen partial pressure.

## Analysis of Microstructural Effect in Oxidation

Oxidation of  $\text{ZrB}_2+\text{SiC}$  produces a complex scale structure containing at least two condensed phases:  $\text{ZrO}_2$  (c) which has highly porous skeleton with percolating holes, and a silica-rich liquid phase that wets the skeleton. Gas species of the greatest interest are  $\text{B}_2\text{O}_3$ , SiO and CO, although BO,  $\text{B}_2\text{O}_2$ ,  $\text{B}_2\text{O}$  etc. are also present and can play important roles in mass transport. SiO could evolve by for instance:  $2\text{SiO}_2$  (l)  $\rightarrow$   $2\text{SiO}$  (g) +  $\text{O}_2$ , which is a key reaction that has been used in constructing volatility diagrams. When in contact with  $\text{SiO}_2$  (l), with decreasing oxygen chemical potential or the equivalent partial pressure, SiO will have higher equilibrium vapor pressure. Volatility diagram of the  $\text{ZrB}_2+\text{SiC}$  system indicates that when  $T > T_B = 1775^\circ\text{C}$ , the peak equilibrium vapor pressure of SiO inside the scale could exceed 1 atm, which would then induce a boiling transition (gas bubbles can nucleate and grow inside the liquid). This violently disrupts the  $\text{SiO}_2$  (l) scale in the case of oxidizing monolithic SiC. However, the scales of  $\text{ZrB}_2+\text{SiC}$  and  $\text{HfB}_2+\text{SiC}$  appear to be much more tolerant of such a boiling transition. It is precisely in this  $T > T_B$  regime that  $\text{ZrB}_2+\text{SiC}$  and  $\text{HfB}_2+\text{SiC}$  demonstrate oxidation resistance superior to monolithic SiC.

We suggest a "dynamic view" and a "steady-state view" of why  $\text{ZrB}_2+\text{SiC}$  is superior to monolithic SiC. The two views are inherently consistent. Imagine a  $\text{ZrB}_2+\text{SiC}$  specimen is gradually being heated up in an oxygen-rich environment like normal air ( $P_{\text{O}_2}=0.2$  atm), initially from  $T \ll T_B$ . At such high ambient  $P_{\text{O}_2}$ , a protective  $\text{SiO}_2$  (l) film will condense on top from the very beginning, that wets the  $\text{ZrO}_2$  (c) skeleton, leaving no voids at the base. At  $T < T_B$ , monolithic SiC in fact resist oxidation better than  $\text{ZrB}_2+\text{SiC}$ . Also at  $T < T_B$ , the  $P_{\text{SiO}}$  branch of the volatility diagram in contact with  $\text{SiO}_2$  (l) has a formal thermodynamic definition but is not physically realizable as pure SiO gas bubbles, because any SiO gas bubble anywhere will be crushed by the dual forces of surface tension and hydrostatic pressure, which we take to be 1 atm inside  $\text{SiO}_2$  (l). However, as the temperature is brought up to  $T > T_B$ , a sharp transition happens inside  $\text{SiO}_2$  (l). Now SiO gas bubbles can nucleate at the base, with  $P_{\text{SiO}}-1\text{atm} > 0$  working against the surface tension. The dynamic view examines how the gas bubbles grow and coalesce, paying attention to the role of the  $\text{ZrO}_2$  (c) skeleton.



The  $\text{ZrO}_2$  (c) skeleton will regulate gas bubble dynamics. Unlike unconstrained growth inside a completely liquid scale, gas bubbles ( $\text{SiO}$ ,  $\text{CO}$ ,  $\text{B}_2\text{O}_3$ ,  $\text{BO}$ ,  $\text{O}_2$  etc. mixture) in a semi-solid porous scale are forced to grow into long fingers (a pressure difference of the order atm is large enough to displace a liquid, but usually not enough to displace a solid). Reaction  $2\text{SiO}_2$  (l)  $\rightarrow$   $2\text{SiO}$  (g) +  $\text{O}_2$  could then happen on one end of the gas finger,  $\text{BO}$ ,  $\text{B}_2\text{O}_3$ ,  $\text{SiO}$ ,  $\text{CO}$  etc. would then diffuse along the gas finger with  $\text{O}_2$  diffusing in the opposite direction, and finally when  $P_{\text{O}_2}$  gets high enough,  $\text{SiO}$  could get re-oxidized to form  $\text{SiO}_2$  (l) on the other end of the finger, and  $\text{B}_2\text{O}_3$  etc. would get solvated in the liquid and continue to diffuse up the scale. This is equivalent to a channeling transfer of  $\text{SiO}_2$  (l) from one end of the finger to the other, which is mechanically untenable without the support and constraint of the  $\text{ZrO}_2$  (c) skeleton. In reality the pores are tortuous instead of straight, giving the effusing  $\text{SiO}$  (g) much opportunity to react with  $\text{O}_2$  (g) near the end, and the  $\text{SiO}_2$  (l) product collected on the  $\text{ZrO}_2$  (c) substrate. The skeleton may also impart significant mechanical integrity to the scale in the case of bubble outbreaks (bubble diameter constrained by the pore diameter) or under external shear flow, since  $\text{SiO}_2$  (l) adheres strongly to a highly porous  $\text{ZrO}_2$  (c) skeleton by capillary forces across a large contact area. In short, the dynamical view is that the  $\text{ZrO}_2$  (c) skeleton helps to collect and retain the silica-rich liquid, playing an important mechanical role.

There is also a "steady-state" explanation, beginning with the interpretation of volatility diagrams. Volatility diagrams represent chemical equilibria when assuming some volatile gas species are in contact with certain condensed phases - solid or liquid. Solid or liquid makes a difference here, because a liquid could flow in or flow out, easily retreating from a region if necessary. If a certain condensed phase retreats, then an originally high volatile gas pressure - assuming the condensed phase was there - loses its significance. This understanding of the volatility diagram may be translated into the following rule: liquid phases will retreat from the region where some volatile gas species, were they in contact, will have high vapor pressure (approaching hydrostatic pressure inside the liquid), to region of lower vapor pressure according to the volatility diagram; after the retreat, the actual vapor pressure of the volatile gas species will be automatically lowered than what the volatility diagram has originally indicated for the evacuated region.

The above rule comes from thermochemistry. Applying the rule to oxidizing monolithic  $\text{SiC}$  above  $T_B$ , we see that the only thermochemically sound steady-state arrangement is for  $\text{SiO}_2$  (l) to retreat to the low  $P_{\text{SiO}}$  - high  $P_{\text{O}_2}$  region, and let gas-phase diffusion take over in the intervening gap, where there will be no condensed liquid phase, thus shutting down the high gas volatility. Unfortunately, although this setup is thermochemically and diffusion-kinetically sound, it is obviously mechanically unstable. The "scale" would easily shear off or spall. This is fundamentally because in monolithic  $\text{SiC}$ , with only a single condensed-phase oxide product, which is a liquid, there is no way to satisfy both thermochemical and mechanical stabilities simultaneously at  $T > T_B$ .

In contrast, when oxidizing  $\text{ZrB}_2 + \text{SiC}$ , one gets two condensed-phase oxide products.  $\text{ZrO}_2$  (c) itself has only low volatilities of  $\text{ZrO}$  (g) and  $\text{ZrO}_2$  (g). Furthermore it is a solid. So it does not retreat from the high  $\text{SiO}$  volatility region, maintaining mechanical connection with the main body. The silica-rich borosilicate liquid duly retreats from the high  $\text{SiO}$  volatility region, thereby removing the high  $\text{SiO}$  volatility automatically. This staggered placements of solid and liquid phases at  $T > T_B$ , with internal gas finger diffusion and gas-solid reactions, is both thermochemically and mechanically sound if the  $\text{ZrO}_2$  (c) skeleton is long enough, such that even after the retreat the liquid phase can still hold onto the solid by capillary forces, to have a "solid pillars, liquid roof" architecture as suggested by many experiments. The actual oxidation of  $\text{SiC}$  particles at  $T > T_B$  then occur directly by  $\text{SiC}$  (c) +  $\text{O}_2$  (g)  $\rightarrow$   $\text{SiO}$  (g) +  $\text{CO}$  (g), a gas-solid reaction without going through the liquid phase, which will lead to a porous "SiC-depleted" substrate layer in the  $\text{ZrB}_2 + \text{SiC}$ . The  $\text{ZrO}_2$  (c) "solid pillars" will also grow longer at the base by gas-solid reaction, with  $\text{O}_2$  (g) reactant and  $\text{B}_x\text{O}_y$  (g) product. On the other end of the gas finger, we will have the reverse reaction:  $2\text{SiO}$  (g) +  $\text{O}_2 \rightarrow 2\text{SiO}_2$  (l) which replenishes the "liquid roof".



The above analysis rationalizes why the microstructure of  $\text{ZrB}_2+\text{SiC}$  is important for its oxidation resistance, since the pore sizes of  $\text{ZrO}_2$  (c) might be related to the pre-oxidation SiC particle sizes. As Gasch et al. mentioned, "at 20 volume percent SiC, if the SiC particles are assumed to be small spheres randomly distributed throughout the  $\text{HfB}_2$  matrix, the amount of SiC should be above the percolation threshold. This means that the SiC particles form a network that is interconnected in three dimensions." For a certain fixed volume fraction, smaller pores and better connectivity inside  $\text{ZrO}_2$  (c) could enhance the collection and retention of the silica-rich liquid. Thus, nanoscale SiC particles might improve the oxidation resistance of  $\text{ZrB}_2+\text{SiC}$ , by refining the microstructure of the in situ formed  $\text{ZrO}_2$  (c) skeleton<sup>1</sup>.

The proposed view also explains why 70-80 vol% of the composite is dedicated to  $\text{ZrB}_2$ . It is seen that a porous  $\text{ZrO}_2$  could be advantageous for the oxidation resistance for a mechanical reason (not a diffusion kinetics one), if there is also a liquid oxide product phase to "collaborate" with. The porous skeleton needs to be strong enough as well as sufficiently long, to have enough room for the liquid oxide phase to retreat outward. Otherwise, the two phases may still have to separate ("high volatility blows away the liquid roof"), and the entire system would lose oxidation protection. One cannot have too much SiC (and thus the liquid) and not enough oxide skeleton, and maintain the mechanical and thermochemical stabilities of the "solid pillars, liquid roof" architecture. Since capillary force holds the solid and liquid phases together, microstructural refinement of the oxide scale will lead to stronger capillary adhesion per unit volume, which could lead to significant improvement of the overall oxidation resistance.

### Modeling of Oxygen Transport in Silica-Rich Liquid

From the above analysis, we see that if  $\text{ZrO}_2$  (c) has a percolating-holes microstructure, the borosilicate liquid will define the effective barrier against oxygen, irrespective of whether fully dense  $\text{ZrO}_2$  is intrinsically better barrier (in open-circuit condition) against oxygen or not than the borosilicate liquid, as the liquid occupies both serial and parallel oxygen transport pathways in the "solid pillars, liquid roof" architecture. In this section we focus on the atomic-level events that govern oxygen transport in the borosilicate liquid.

Experimentally, it is still challenging to accurately determine the composition profile of the borosilicate liquid because boron is a light element. According to the Hertz-Knudsen-Langmuir equation, the net evaporation flux of a species from a liquid surface is proportional the difference between the equilibrium vapor pressure and the actual vapor pressure of the species at the surface. Since pure  $\text{B}_2\text{O}_3$  (l) has much higher equilibrium vapor pressure than pure  $\text{SiO}_2$  (l) in an oxygen-rich environment, a borosilicate liquid facing air would preferentially evaporate  $\text{B}_2\text{O}_3$  instead of  $\text{SiO}_2$ . Thus the borosilicate liquid should be overall silica rich, with a composition gradient that is  $\text{B}_2\text{O}_3$ -depleted at the liquid-air interface, and  $\text{B}_2\text{O}_3$ -enriched at the gas finger-liquid interface, as  $\text{B}_2\text{O}_3$  (g) and other boron-bearing gas species are carried along with  $\text{SiO}$  (g) in the gas finger and get absorbed into the liquid. Previously, Bongiorno and Pasquarello have studied oxygen transport in pure silica glass using a multiscale modeling approach that combines high-level quantum mechanical (DFT) calculations of the diffusing oxygen species and local energy barriers, with kinetic Monte Carlo sampling of connected migration pathways. To bound the results, we decide to model a borosilicate liquid composition of equal  $\text{B}_2\text{O}_3$  and  $\text{SiO}_2$  proportions.

One major challenge in modeling any glass or liquid is to have reliable atomic structures. We have adopted the structure generation approach of Van Ginhoven, Jonsson and Corrales, which was shown to reproduce experimental pair distribution functions for pure silica. The approach requires a classical interatomic potential to perform long-time molecular dynamics (MD) simulations at the beginning, followed by further DFT optimizations. To generate the classical potential, we adopt the van Beest, Kramer and van Santen (BKS) parameterization for Si-O interactions, but fit B-O and Si-B interactions to a series of small DFT calculations for bulk  $\text{B}_2\text{O}_3$ , using the software package GULP. Then, starting from random positions for oxygen, boron and silicon atoms in the supercell, we perform a sequence of classical MD simulations at temperatures 6000, 5000, 4000, 3000, 2000 and 1000 K. The resulting

<sup>1</sup>S. S. Hwang, A. L. Vasiliev, and N. P. Padture, *Materials Science and Engineering A*, 464 (2007) 216-224.



structures were then used as input geometries for further DFT calculations (Vienna ab-initio simulation program with spin-polarized PW91 functional, projector augmented wave method, planewave kinetic energy cutoff 400 eV). For our initial studies, a cubic supercell containing  $14 \text{ SiO}_2 + 7 \text{ B}_2\text{O}_3$  formula units is used, with total 77 atoms. The average density is  $2.3 \text{ g/cm}^3$ . A typical liquid structure at  $T = 2500^\circ\text{C}$ , after further equilibration by ab initio MD, clearly has a framework structure with no dangling bonds (all Si are 4-fold coordinated to O, and all B are 3-fold coordinated to O).

Based on these atomic structures, we have studied the thermodynamic stability and diffusion kinetics of solvated oxygen molecules  $\text{O}_2^*$  and atomic  $\text{O}^*$  in borosilicate liquid. The former stay inside the open cages of the framework and do not interact chemically with the framework. The latter are chemically incorporated into the network in the form of peroxy linkage Si-O-O-B, extra bridging O between two B, and others. Since diffusion could be a rare event, simply performing molecular dynamics simulations and tracking the mean squared displacements may not be sufficient, and energy-landscape exploration techniques such as nudged elastic band (NEB) calculations may be needed. These methods compute the minimum energy path (MEP) and saddle-point configuration of thermally activated processes, and then use transition-state theory to estimate the rates.

First, we place one  $\text{O}_2^*$  inside a cage and perform DFT molecular dynamics simulation at  $2500^\circ\text{C}$  for 11 picoseconds. It is very clear from the MD trajectory (in contrast to those of simple liquids such as Ar, as well as water) that the borosilicate liquid still maintains a very "rigid" framework at  $2500^\circ\text{C}$ . Indeed, pure silica is a strong glass-forming liquid, and its viscosity does not show a precipitous drop above the glass transition temperature. For instance, even at  $2500^\circ\text{C}$ , pure silica still has a shear viscosity  $\sim 10^4$  Poise, which is a million times thicker than that of room-temperature water. This means the liquid still has a well-defined network structure at any given moment, and its topological change does not occur at the same timescale as, for instance, its own Si-O-Si bond stretching. Also, from the 11 picoseconds ab initio MD trajectory, we find the  $\text{O}_2^*$  is essentially trapped inside one cage. It just bounces back and forth many times inside a jiggling cage, with no possibility of escape within the MD simulation timescale. These facts suggest that one is still justified to use transition-state theory and numerical schemes like the nudged elastic band (NEB) method to characterize diffusion of  $\text{O}_2^*$ , despite it is embedded in a liquid. From our MD simulations, adding 50%  $\text{B}_2\text{O}_3$  to silica does not seem to change this consideration qualitatively.

A complication for the NEB calculation is that unlike in crystals, diffusion inside an amorphous framework has a distribution of local minima and activation energies. Not all cages have the same volume, nor the same energy for opening up the constrictions when  $\text{O}_2^*$  squeezes from one cage into the other. In Fig. 5 of <sup>2</sup>, we have shown a typical DFT-NEB calculated minimum energy path of  $\text{O}_2^*$  diffusion (vehicular diffusion mode). The forward hop barrier is 1.8 eV, whereas the backward hop barrier is 1.4 eV. These are somewhat higher than the 1.12 eV effective migration barrier that Bongiorno and Pasquarello predicted for  $\text{O}_2^*$  vehicular diffusion in pure silica, perhaps because of the  $\text{B}_2\text{O}_3$  modifications to the network. More calculations are needed in order to have better statistics.

For vehicular diffusion inside a liquid, there is a well-known Stokes-Einstein relation where one correlates diffusivity to the inverse of viscosity. Even though the Stokes-Einstein relation is quite successful in simple liquids, it can fail in network-forming liquids. Norton measured the permeation of gaseous oxygen through vitreous silica and found an activation energy of 27 kcal/mol (1.17 eV) for  $D(\text{O}_2^*)$ , in substantial agreement with later measurements. However, the activation energy governing the viscosity of vitreous silica, is in the range of 5.3 to 7.5 eV. So clearly the Stokes-Einstein relation does not work here. From our DFT modeling, the physics governing the activation energy of  $\text{O}_2^*$  vehicular diffusion is seen to be an elastic deformation of the framework (elastic opening of the constrictions) without changing its network topology. But the physics behind the activation energy of must involve network topology changes, which necessarily involve Si-O bond breaking.

<sup>2</sup>A. Bongiorno, C. J. Forst, R. K. Kalia, J. Li, J. Marschall, A. Nakano, M. M. Opeka, I. G. Talmy, P. Vashishta, and S. Yip, MRS Bulletin, 31 (2006) 410-418.



In addition to  $O_2^*$  vehicular diffusion, oxygen transport may also occur by Grotthuss-type oxygen-hopping mechanisms, mediated by network defects such as peroxy linkage or oxygen deficient centers. These mechanisms would involve bond breaking, and typically higher effective activation energies - mostly due to the formation energies of such defects. One such pathway involves an  $O_2^*$  breaking up into two  $O^*$ :  $O_2^* \rightarrow O^* + O^*$ . The two  $O^*$ s then move independently of each other for a while, and eventually recombine on the other side of the cage in this particular NEB calculation setup.

We find from multiple NEB calculations in the borosilicate framework that these coordination defects, once formed, can interconvert easily, suggesting low migration barriers, similar to interstitial defects in metals. Furthermore, there are two free translational centers: the two  $O^*$ s, once formed, can move independently of each other inside the liquid. The  $O_2^*$  vehicular diffusion has only one free translational center, in order to maintain its molecular form. Thus diffusion by  $O_2^* \rightarrow O^* + O^*$  has entropic advantage of approximately  $k_B \ln c$ , where  $c$  is the prevalent oxygen carrier concentration (per formula unit of  $SiO_2 + B_2O_3$ ), whereas the  $O_2^*$  vehicular diffusion has energy advantage. The classic enthalpy-entropy tradeoff in free energy then suggests that there exists a temperature  $T_C$ , below which  $O_2^*$  is dominant in concentration, and above which  $O^*$ s are dominant, if the borosilicate is in an oxygen-rich environment (the equivalent  $P_{O_2}$  is high). In lower equivalent  $P_{O_2}$  environment, oxygen deficient centers are also possible carriers.

In reference to  $O_2$  in the gas phase, we find the average potential energy of  $O_2^*$  solvated in borosilicate is 0.73 eV per molecule, which is essentially the elastic energy in the framework needed to accommodate the molecule. The average potential energy of  $O^*$ , on the other hand, is about 1.78 eV per O. These energies are used to compute the concentration of  $O_2^*$  and  $O^*$  in borosilicate in equilibration with  $P_{O_2} = 0.1$  atm. Note that  $c(O_2^*)$  scales linearly with  $P_{O_2}$ , whereas  $c(O^*)$  scales linearly with  $P_{O_2}^{1/2}$ . Thus, deeper and deeper into the scale, as the oxygen chemical potential gets lower and lower, the Grotthuss-type oxygen transport should become relatively more and more important.

Norton measured the solubility of  $O_2^*$  in pure silica at 1078°C and  $P_{O_2} = 1$  atm to be  $1.9 \times 10^{-3}$  cm<sup>3</sup> STP  $O_2$  gas per cm<sup>3</sup> silica. This amounts to  $5.1 \times 10^{16}$  per cm<sup>3</sup> silica or a dimensionless concentration of about  $c = 10^{-5}$ , at  $P_{O_2} = 1$  atm. This is about two orders of magnitude higher than our DFT predicted  $O_2^*$  solubility in borosilicate. This could be due to the structural difference between pure silica framework and borosilicate framework. As Bongiorno and Pasquarello noted, the potential energy of  $O_2^*$  depends sensitively on the cage interstice volume, and there is certainly a structural difference between pure silica and  $B_2O_3$  modified networks. This could also be partly due to the intrinsic errors of PW91 density functional, which are known to give large errors treating isolated molecules (the reference state), and non-bonding interactions ( $O_2^*$  interactions with the framework).

The above uncertainties aside, it is still a rather conservative estimate that above  $T_C \sim 1500^\circ\text{C}$  the dominant oxygen carriers in the borosilicate "liquid roof" are network defects instead of molecular  $O_2^*$ , because there are other factors that disfavor the Deal-Grove mechanism: (a) the DFT calculations indicate that the  $O^*$ s not only have entropy advantage, but also mobility advantages over  $O_2^*$ , (b) intense aerothermal heating environment may introduce a significant level of dissociated oxygen on the outer liquid surface, which would favor  $O^*$  diffusion from a non-equilibrium kinetics perspective, (c) as  $P_{O_2}$  drops from  $\sim 10^4$  Pa on the outer liquid surface to less than  $10^{-5}$  Pa equivalent at the internal gas finger-liquid interface according to the volatility diagram, the balance will shift more and more away from  $O_2^*$  vehicular diffusion to network defect Grotthuss diffusion. Oxygen deficient centers may play a significant role in oxygen transport at low equivalent  $P_{O_2}$ s. It seems plausible that oxygen in the borosilicate liquid could react with the underlying substrate or SiO (g), injecting oxygen vacancies (e.g. regions of high B and Si stoichiometry) into the liquid, which then diffuse up the scale to recombine with  $O_2^*$  or  $O^*$  somewhere inside the liquid. (d) In all the DFT calculations, we have only considered neutral network defects. Charging the defects may significantly greatly reduce their formation energies, although we will then need to solve the complementary problem of what other defects compensate the charge and carry out ambipolar diffusion under open-circuit condition.



The mobility advantage of the peroxy linkage over  $O_2^*$  suggests that arc-jet testing, which introduces a non-equilibrium distribution of dissociated oxygen atoms on the surface, will likely lead to faster oxidation than ordinary furnace testing at the same temperature. Also, because the network defects are chemically incorporated into the network and thus interact more strongly with solutes than  $O_2^*$ , small changes in the glass chemistry could lead to large changes in the oxygen diffusivity by defect trapping/gettering.

### Summary

We present a congruent explanation of the oxidation protection of  $ZrB_2+SiC$  based on a "solid pillars, liquid roof" scale architecture, where the borosilicate liquid defines the effective diffusion barrier, and the solid zirconia collects and retains the liquid and provides mechanical support. Internal gas fingers will form as the liquid phase retreats to remove the high  $SiO$  volatility above a boiling transition temperature. At such high temperatures, to satisfy both thermochemical and mechanical stabilities, the "solid pillars, liquid roof" architecture seems to be a viable solution, not available to monolithic  $SiC$ .

Compared to the borosilicate liquid phase, whether fully dense zirconia is blocking or unblocking to oxygen in open-circuit condition depends on its electronic conductivity (transference number), which in turn depends on how the charge defects are compensated inside the crystal, related to the amount of impurities. If the zirconia phase has a highly porous microstructure, however, then the above discussion is likely irrelevant and the borosilicate liquid phase will control the effective diffusion barrier, since it will occupy both serial and parallel oxygen transport pathways.

At low temperatures, it is commonly accepted that molecular oxygen  $O_2^*$  dominates oxygen transport. However, from first-principles calculations with detailed borosilicate atomic structures, it seems unlikely that this will remain the case at temperatures of practical interest for the  $ZrB_2+SiC$  thermal protection system (above  $1500^\circ C$ ). This means that the oxidation rate will likely have a complex, sub-linear dependence with respect to the external oxygen partial pressure. Also, if the oxygen carriers are chemically incorporated and interact strongly with the framework, there is hope that by tuning the glass composition, the carriers could be trapped, thereby slowing down oxygen diffusion.

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### Personnel Supported by the Project

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### Presentations

Invited talk, NIST 2008 Diffusion Workshop, Gaithersburg, Maryland, May 12-13, 2008.

Invited talk, TMS 2008 Annual Meeting & Exhibition, New Orleans, March 9-13, 2008.

Invited talk, International Workshop on Small Scale Plasticity, Braunwald, Switzerland, September 5-8, 2007.

Keynote talk (45 min), ninth U.S. National Congress on Computational Mechanics (USNCCM IX), San Francisco, July 22-26, 2007.

Invited seminar at Department of Aerospace and Mechanical Engineering, University of Notre Dame, March 20, 2007.

Los Alamos National Lab Physics & Theoretical Colloquium, March 15, 2007, 2007.

Invited talk, Center for Advanced Metallic and Ceramic Systems (CAMCS) Seminar, Johns Hopkins University, Baltimore, Maryland, January 3, 2007.

Invited talk, Pacific Northwest National Laboratory, Richland, WA, September 15, 2006.

Invited talk, 232nd ACS National Meeting, San Francisco, September 10-14, 2006.

MRS OYI presentation, San Francisco, April 19, 2006.

## Publications

1. A. Samanta, T.J. Lenosky and J. Li, "Thermodynamic stability of point defects in cubic zirconia," manuscript in preparation.
2. C.J. Först, J. Li, A. Samanta, P. E. Blöchl and S. Yip, "Defect Chemistry on a Grid: A First-Principles Toolkit," manuscript in preparation.
3. J. Li, T.J. Lenosky, C.J. Först and S. Yip, "Thermochemical and Mechanical Stabilities of the Oxide Scale of ZrB<sub>2</sub>+SiC and Oxygen Transport Mechanisms," *J. Am. Ceram. Soc.* **91** (2008) 1475-1480.
4. A. Bongiorno, C.J. Först, R.K. Kalia, J. Li, J. Marschall, A. Nakano, M.M. Opeka, I.G. Talmy, P. Vashishta and S. Yip, "A Perspective on Modeling Materials in Extreme Environments: Oxidation of Ultra-High Temperature Ceramics," *MRS Bulletin* **31** (2006) 410-418.
5. H. Kimizuka, S. Ogata and J. Li, "Hydrostatic compression and high-pressure elastic constants of coesite silica," *J. Appl. Phys.* **103** (2008) 053506.
6. T. Zhu, J. Li, A. Samanta, A. Leach and K. Gall, "Temperature and Strain-Rate Dependence of Surface Dislocation Nucleation," *Phys. Rev. Lett.* **100** (2008) 025502. Cover article.
7. H. Mori, S. Ogata, J. Li, S. Akita and Y. Nakayama, "Plastic bending and shape-memory effect of double-wall carbon nanotubes," *Phys. Rev. B* **76** (2007) 165405.
8. F. Liu, P.B. Ming and J. Li, "Ab initio calculation of ideal strength and phonon instability of graphene in tension," *Phys. Rev. B* **76** (2007) 064120.
9. Y.M. Wang, J. Li, A.V. Hamza and T.W. Barbee, Jr., "Ductile crystalline-amorphous nanolaminates," *Proc. Natl. Acad. Sci. USA* **104** (2007) 11155-11160.
10. A. Gouldstone, N. Chollacoop, M. Dao, J. Li, A. Minor and Y.-L. Shen, "Indentation Across Size Scales and Disciplines: Recent Developments in Experimentation and Modeling," *Acta Mater.* **55** (2007) 4015-4039. Overview No. 142.
11. H. Kimizuka, S. Ogata, J. Li and Y. Shibutani, "Complete set of elastic constants of alpha-quartz at high pressure: A first-principles study," *Phys. Rev. B* **75** (2007) 054109.
12. T. Zhu, J. Li, A. Samanta, H.G. Kim and S. Suresh, "Interfacial Plasticity Governs Strain Rate Sensitivity and Ductility in Nanostructured Metals," *Proc. Natl. Acad. Sci. USA* **104** (2007) 3031-3036. Cover article.
13. H. Mori, S. Ogata, J. Li, S. Akita and Y. Nakayama, "Energetics of plastic bending of carbon nanotubes," *Phys. Rev. B* **74** (2006) 165418.
14. F. Shimizu, S. Ogata and J. Li, "Yield Point of Metallic Glass," *Acta Mater.* **54** (2006) 4293-4298.
15. C.-Z. Wang, J. Li, K.-M. Ho and S. Yip, "Undissociated screw dislocation in Si: glide or shuffle-set?" *Appl. Phys. Lett.* **89** (2006) 051910.



16. A. Romano, J. Li and S. Yip, "Atomistic simulation of rapid compression of fractured silicon carbide," *J. Nucl. Mater.* **352** (2006) 22-28.
17. S. Ogata, F. Shimizu, J. Li, M. Wakeda and Y. Shibutani, "Atomistic Simulation of Shear Localization in Zr-Cu Bulk Metallic Glass," *Intermetallics* **14** (2006) 1033-1037.
18. X. Lin, J. Li, C. J. Först and S. Yip, "Multiple Self-Localized Electronic States in Trans-Polyacetylene," *Proc. Natl. Acad. Sci. USA* **103** (2006) 8943-8946.
19. T. Zhu, J. Li and S. Yip, "Atomistic characterization of three-dimensional lattice trapping barriers to brittle fracture," *Proc. R. Soc. A* **462** (2006) 1741-1761.
20. X.-F. Qian, J. Li, X. Lin and S. Yip, "Time-dependent density functional theory with ultrasoft pseudopotentials: Real-time electron propagation across a molecular junction," *Phys. Rev. B* **73** (2006) 035408.
21. J. Eapen, J. Li and S. Yip, "Statistical Field Estimators for Multiscale Simulations," *Phys. Rev. E* **72** (2005) 056712.
22. T. Zhu, J. Li and S. Yip, "Nanomechanics of Crack Front Mobility," *J. Appl. Mech.* **72** (2005) 932-935.
23. S. Ogata, J. Li and S. Yip, "Energy landscape of deformation twinning in bcc and fcc metals," *Phys. Rev. B* **71** (2005) 224102.
24. T. Zhu, J. Li, X. Lin and S. Yip, "Stress-dependent molecular pathways of silica-water reaction," *J. Mech. Phys. Solids* **53** (2005) 1597-1623.

#### Awards received

*Technology Review* TR35 award, for 35 "world's top innovators" under age 35 (2007)

National Academy of Engineering U.S. Frontiers of Engineering Symposium (Microsoft Research, Sept. 24-26, 2007), "that brings together 100 of the nation's outstanding young engineers (ages 30-45)"

Materials Research Society (MRS) 2006 Outstanding Young Investigator Award, "for innovative work on the atomistic and first-principles modeling of nanoindentation and ideal strength in revealing the genesis of materials deformation and fracture."

Ohio State University College of Engineering 2006 Lumley Research Award

Presidential Early Career Award for Scientists and Engineers (PECASE) 2005, "in recognition of groundbreaking work in developing multi-scale simulation approaches to studying the mechanics of materials, which has lead to a fundamental understanding of nanomechanics, and for leading new efforts at the interface of nanoscience, biology, and applied mathematics."